

Design of Experiments

Contemporary and Practical Views for Forest Products Manufacturers

A Customized Training Course

by

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